

***Precise α_K Internal Conversion Coefficients
Measurements of 30.77-keV M4 Transition in ^{93m}Nb :
Last Test of Internal Conversion Theory***

TEXAS A&M PROGRAM TO MEASURE ICC

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Internal Conversion Coefficients (ICC):

- Big impact on quality of nuclear science***
- Central for the nuclear data evaluation programs***
- Intensely studied by theory and experiment***
- Important result: hole calculation now standard***

2002RA45 survey ICC's theories and measurements

- **Theory: RHFS and RDF comparison**

Exchange interaction, Finite size of nucleus, *Hole treatment*

- **Experiment:**

100 *E2, M3, E3, M4, E5* ICC values, 0.5%-6% precision,
very few <1% precision!

- **Conclusions, $\Delta(\text{exp:theory})\%$:**

No hole: **+0.19(26)% BEST!**

(bound and continuum states - SCF of neutral atom)

Hole-SCF: **-0.94(24)%**

(continuum - SCF of ion + hole (full relaxation of ion orbitals))

Hole-FO: **-1.18(24)%**

(continuum - ion field from bound wave functions of neutral atom

(no relaxation of ion orbitals))

PHYSICAL ARGUMENT

K-shell filling time vs. time to leave atom

$\sim 10^{-15} - 10^{-17} \text{ s} \gg \sim 10^{-18} \text{ s}$

Overview of the scope and completeness of the method

- **Scope:** *Minimize* ICC measurement unc (~1%) and *maximize* $\Delta_{theory}(\text{FO,NH})\%$ (>4%, *E3, M4*)
- **Completeness:** There is no criterion to reach the scope of comparison between ICC theories “with hole” and “no hole” except for measuring precisely as many relevant cases as practically possible

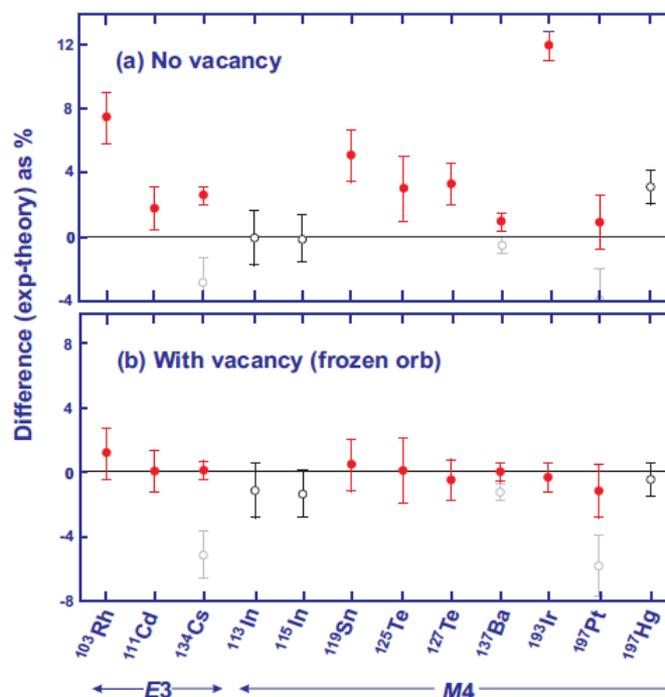
Frozen orbital:
X ray emitted before atomic orbitals have time to rearrange after electron's removal.

Self-consistent field (SCF):
After electron emission, the ion orbitals fully relax before the x ray is emitted.

Comparison of all nine TAMU experimental α_K values with the three theories

Theory	χ^2
with hole (frozen orb.)	1.3
with hole (SCF)	21
no hole	241

OUR RESULTS



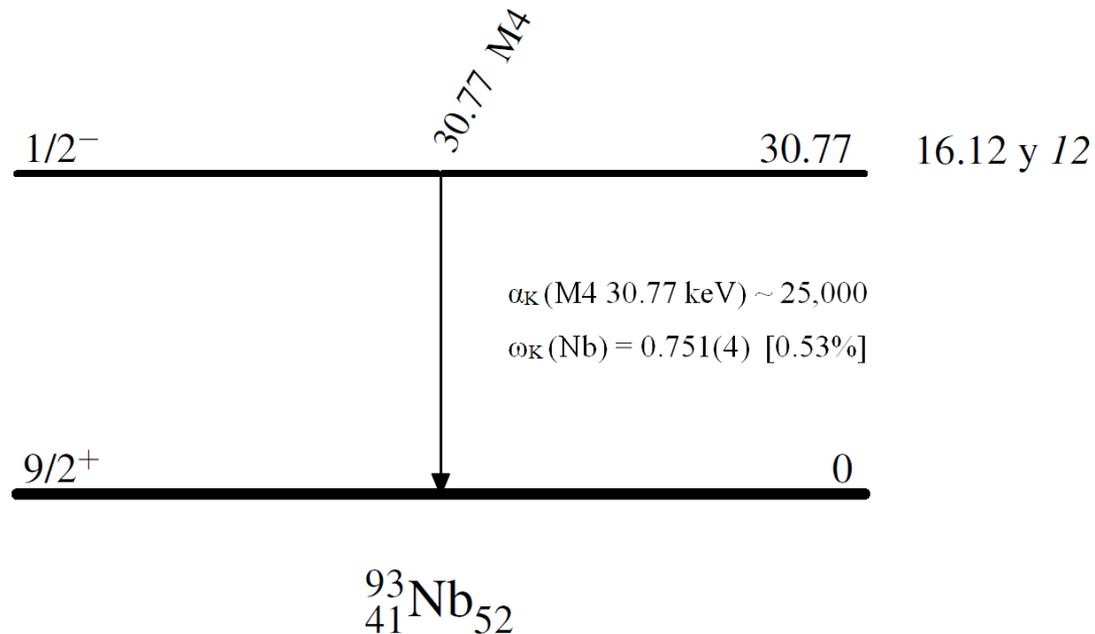
III. ^{93m}Nb 30.77(2) keV, M4 transition

- $\alpha(\text{K})_{\text{exp}}$: 25800 1500 [1], 17000 3000 [2]
- $\alpha(\text{K})_{\text{hole_FO}} = 26000$ 400, $\alpha(\text{K})_{\text{no_hole}} = 23900$ 400,
 $\Delta_{\text{Theory}}(\text{FO,NH}) = 8.5\%$ - *Second most favourable case after ^{193}Ir*

[1] M.Jurcevic, A.Ljubcic, D.Rendic, Fizika 8, 81 (1976)

[2] J.Morel, J.-P. Perolat, N.Coursol, C.R.Acad.Sci., Ser.B 284, 223 (1977)

Decay scheme of ^{93m}Nb (ENSDF)



Texas A&M precision ICC measurements:

- **KX to γ rays ratio method**

$$\beta^- : \alpha_K = \frac{N_K}{N_\gamma} \cdot \frac{\varepsilon_\gamma}{\varepsilon_K} \cdot \frac{1}{\omega_K}$$

- N_K, N_γ measured from *only one K-shell converted transition*
- ω_K from 1999SCZX (compilation and fit)
- **Very precise detection efficiency for ORTEC γ -X 280-cm³ coaxial HPGe at standard distance of 151 mm:**
 - **0.2% , 50-1400 keV**
 - **0.4% , 1.4-3.5 MeV**
 - **~1% , 10-50 keV (KX rays domain)**

Preparation and properties of the $^{93\text{m}}\text{Nb}$ source

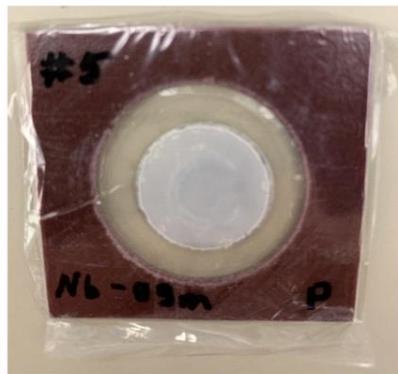
- We purchased a solution of $^{93\text{m}}\text{Nb}$ in 1 M HNO_3 / 0.3 M HF.
- Dr. Tereshatov (from Dr. Folden's group) used *molecular electroplating technique*[†] to deposit Nb on (12 μm thick) aluminum backing in the form of Nb_2O_5 .
- Chemical identity of the source was confirmed by means of Energy Dispersive Spectroscopy (EDS) and X-ray Photoelectron Spectroscopy (XPS), as well as by visual inspection.
- Five sources were prepared, but only the most active one was used in the measurements ($\sim 3.6 \mu\text{Ci}$ of $^{93\text{m}}\text{Nb}$).

[†] D.A. Mayorov, E.E. Tereshatov, T.A. Werke, M.M. Frey, C.M. Folden III, NIMB **407**, 256 (2017).

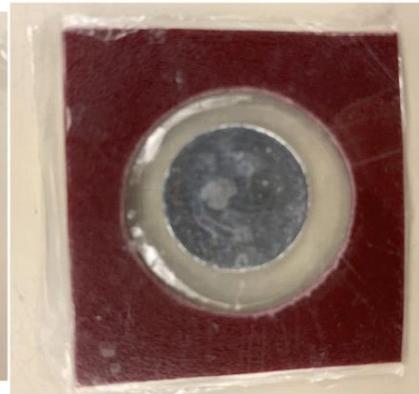
Preparation and properties of the ^{93m}Nb source

- The mounting frame was placed on a big piece of Scotch tape and the backing side of the source was glued onto the exposed tape in the center of the frame.
- The source side was covered with 3.8 μm thick Mylar foil (540 $\mu\text{g}/\text{cm}^2$).

Source side

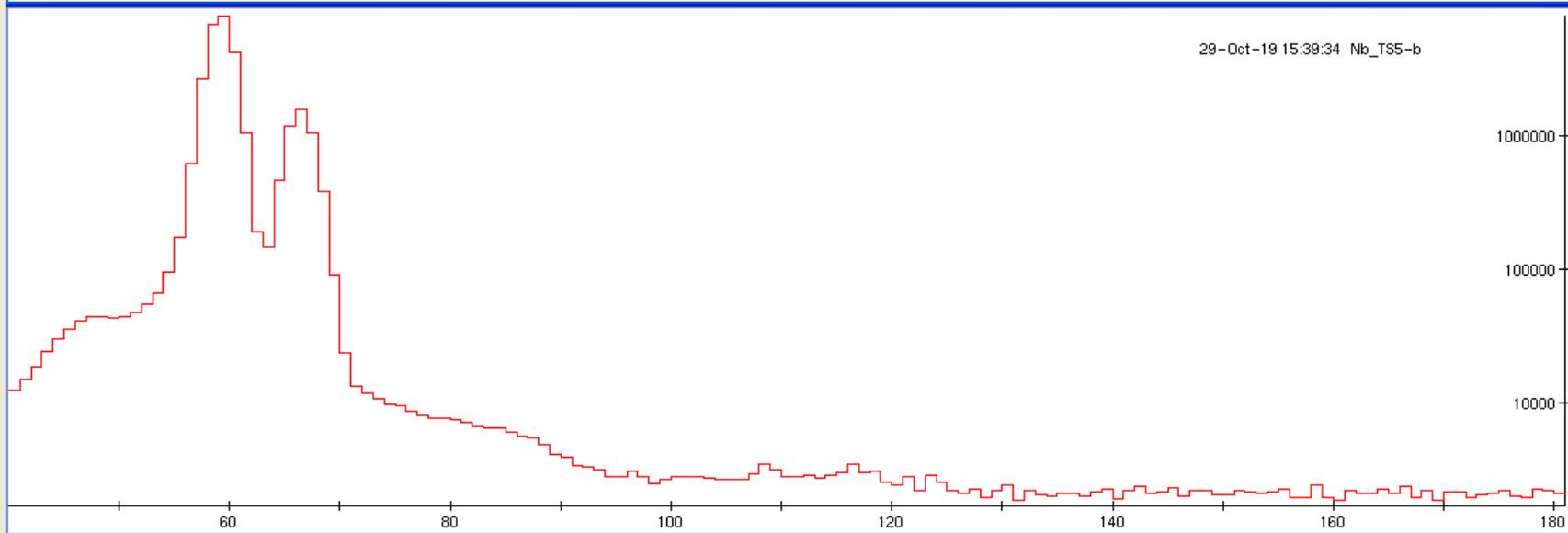
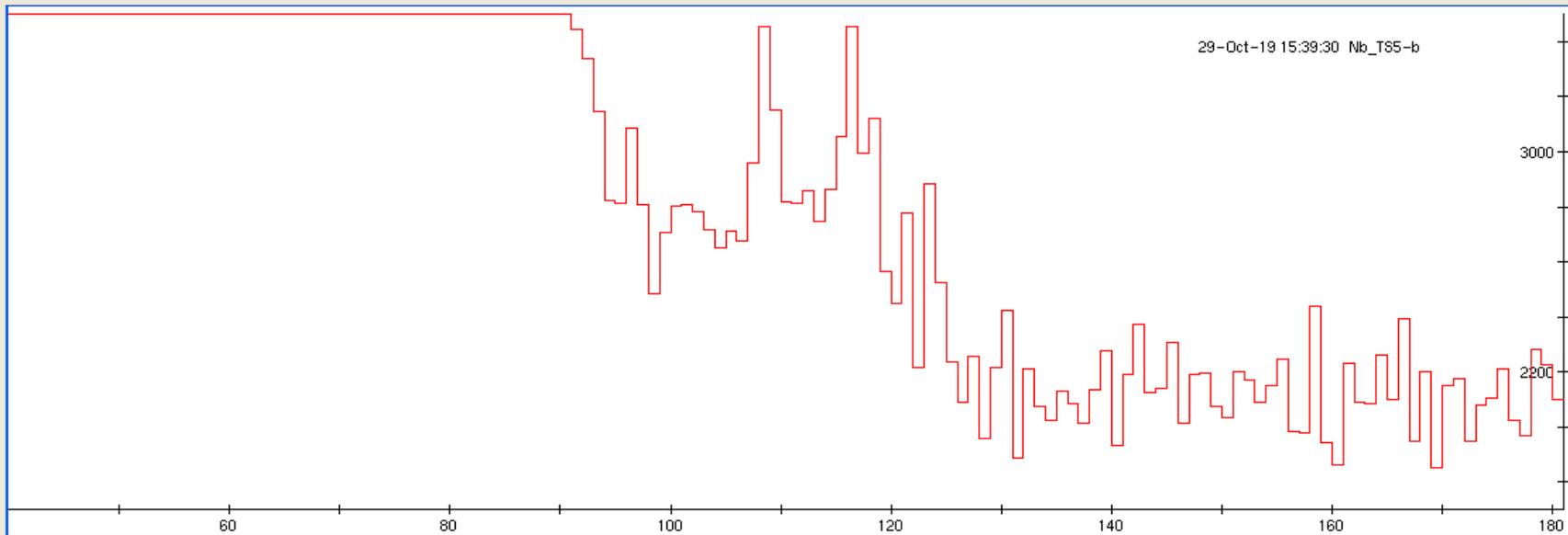


Backing side

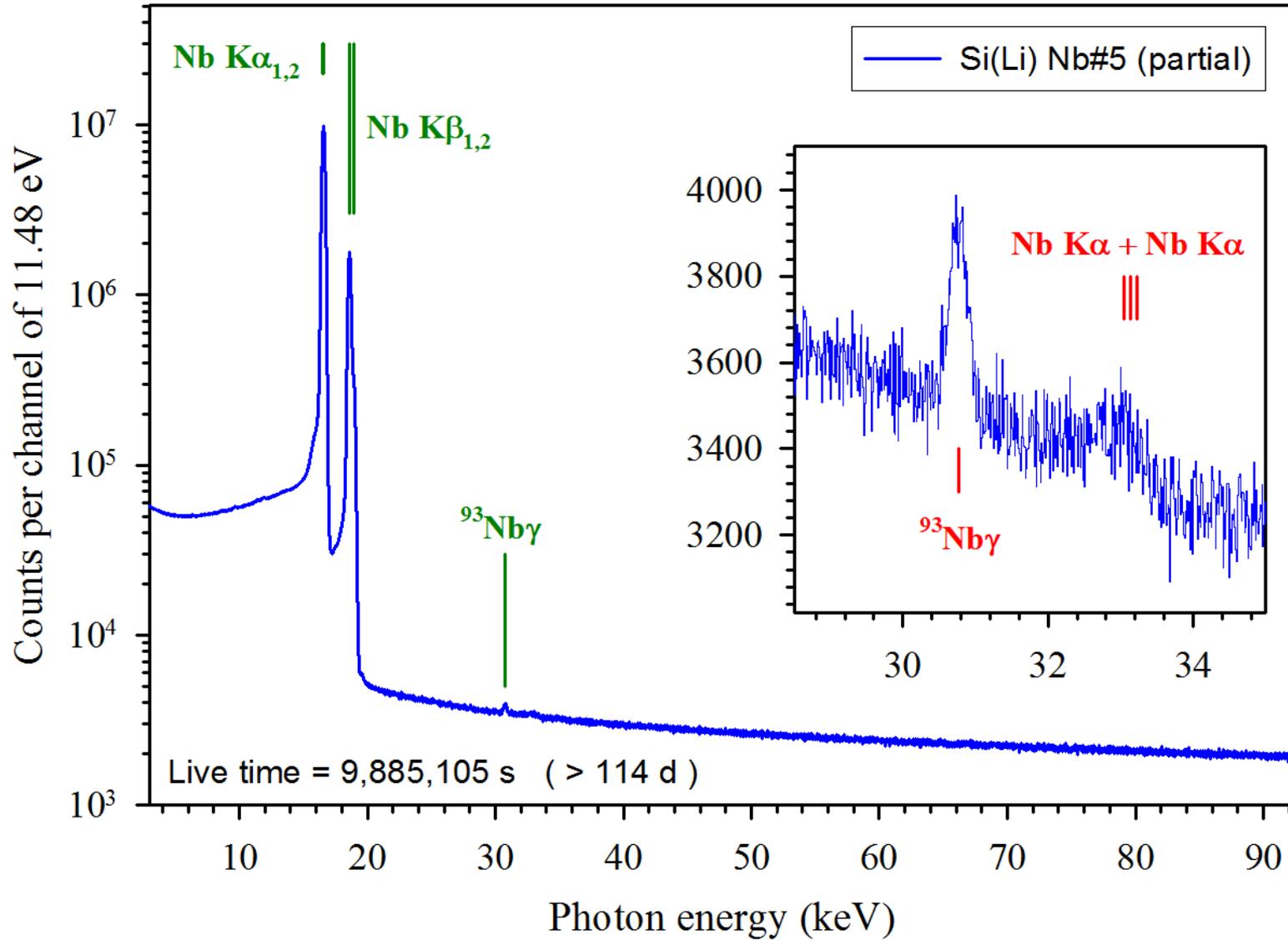


Mass = 3.0 mg, Diameter = 17 mm \implies Mass thickness = 1.3 mg/cm^2

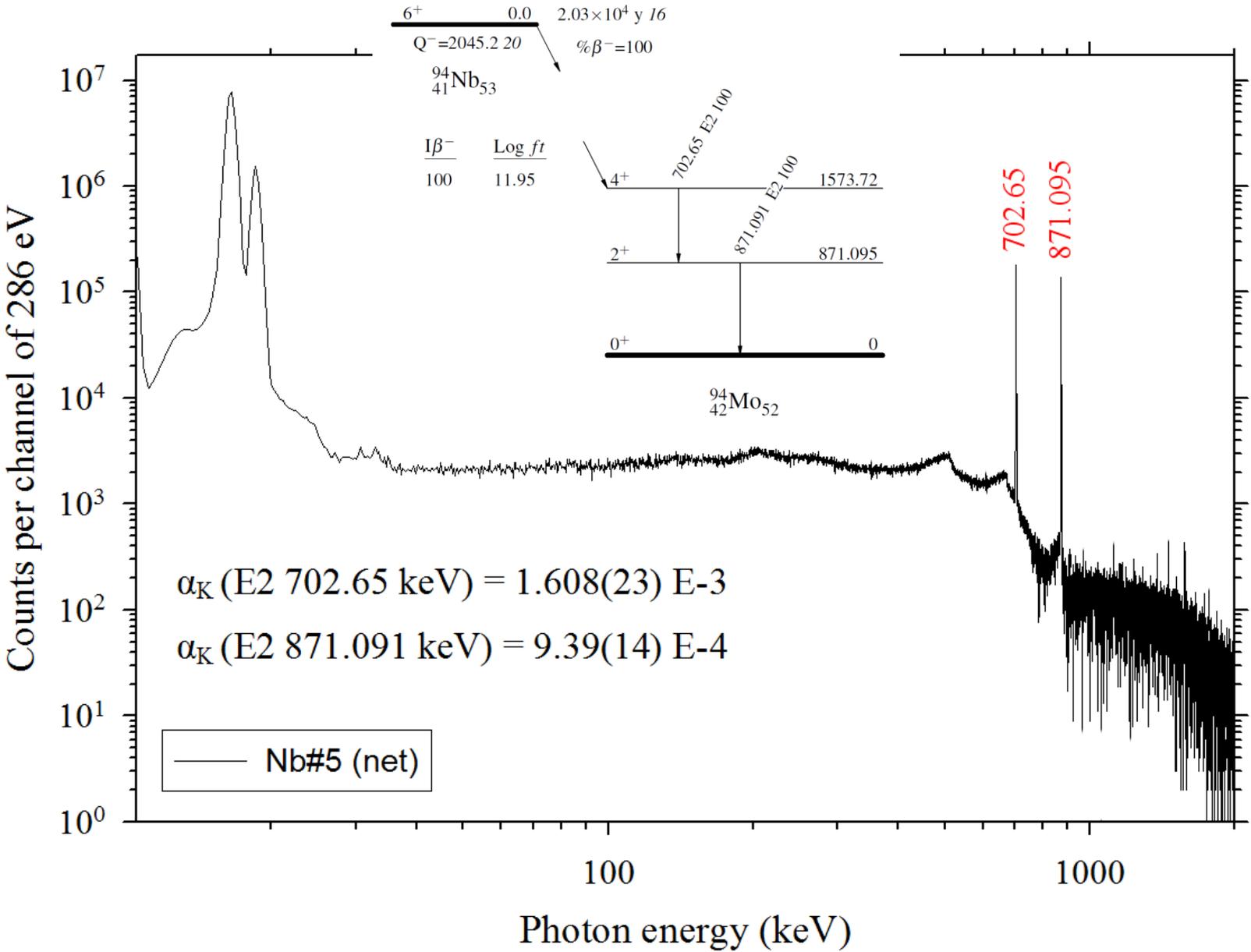
Density (Nb_2O_5) = 4.6 g/cm^3 \implies Thickness = 2.87 μm



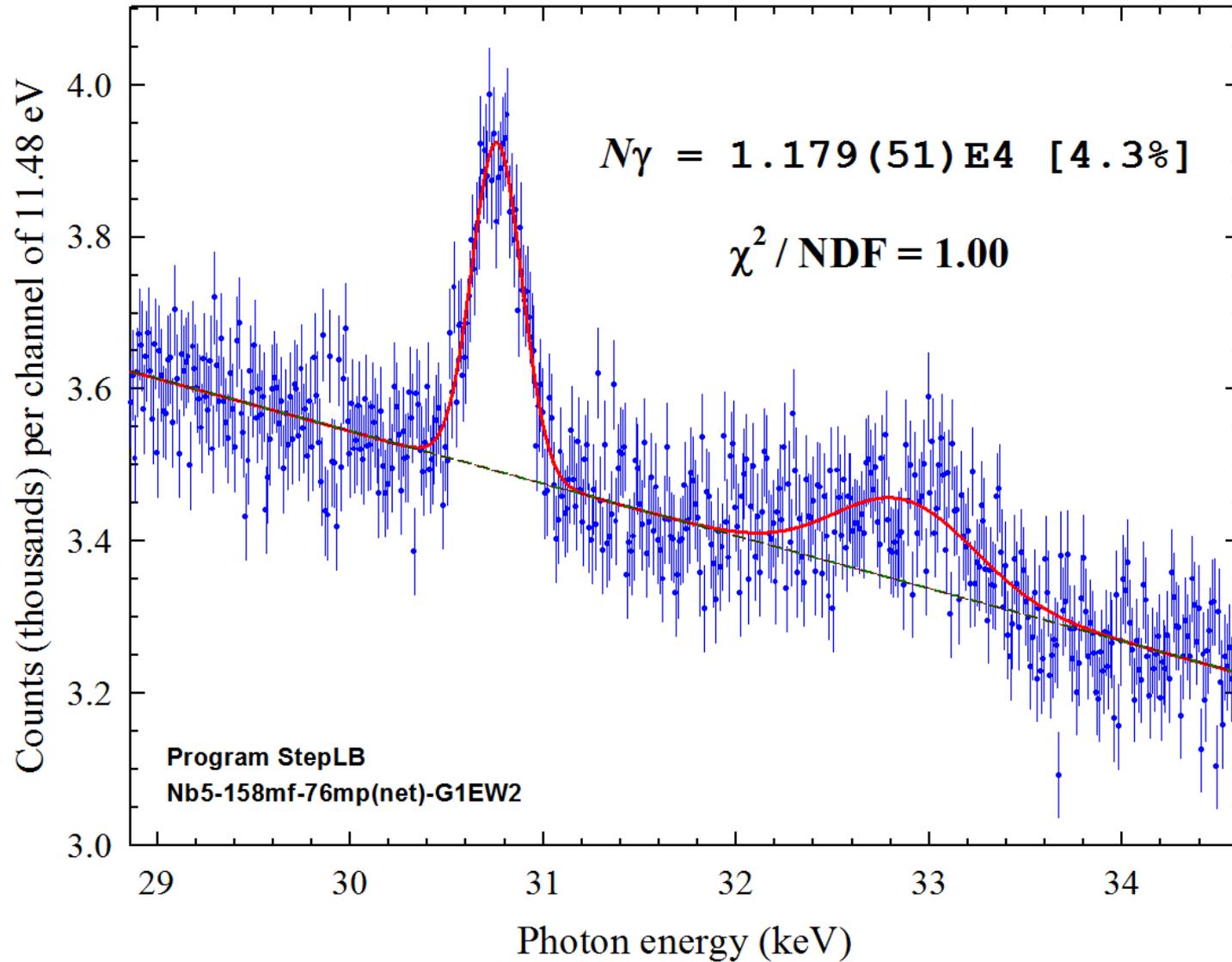
Spectrum measured with the Si(Li) detector



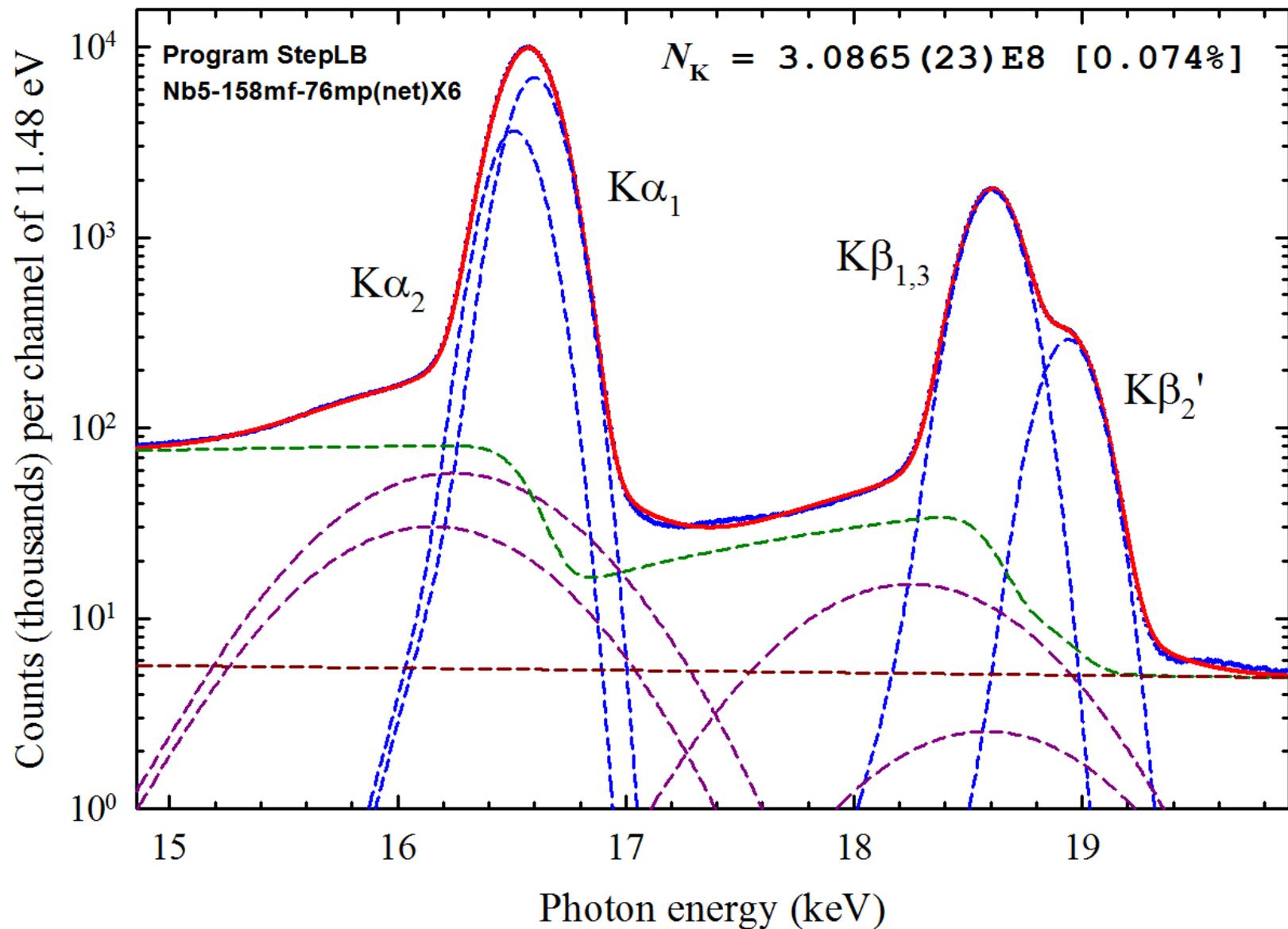
Contaminants in the source



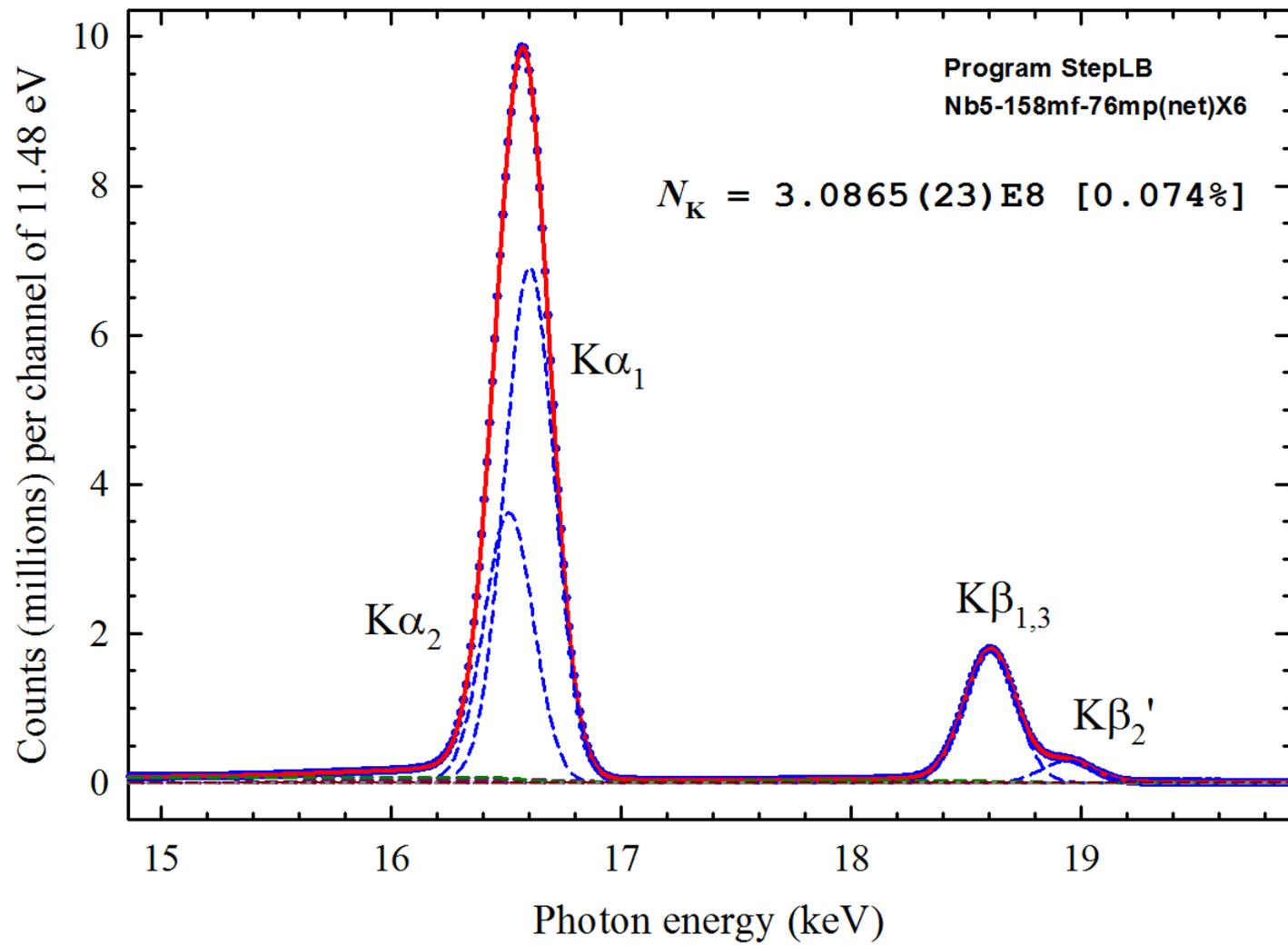
Determination of N_γ



Determination of N_K



Determination of N_K



^{109}Cd Efficiency Calibration

22.6-keV AgKx & 88.0-keV E3 γ regions

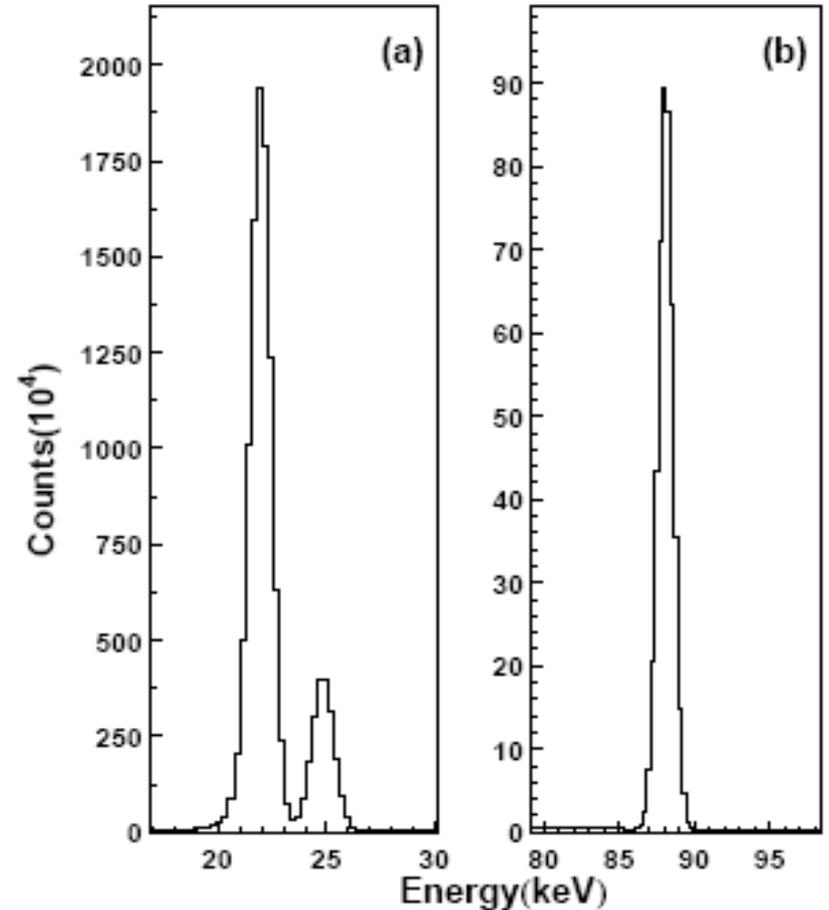
Photopeak efficiency:

^{109}Cd ε Decay: *single 88 γ*

-22.6-keV AgKx

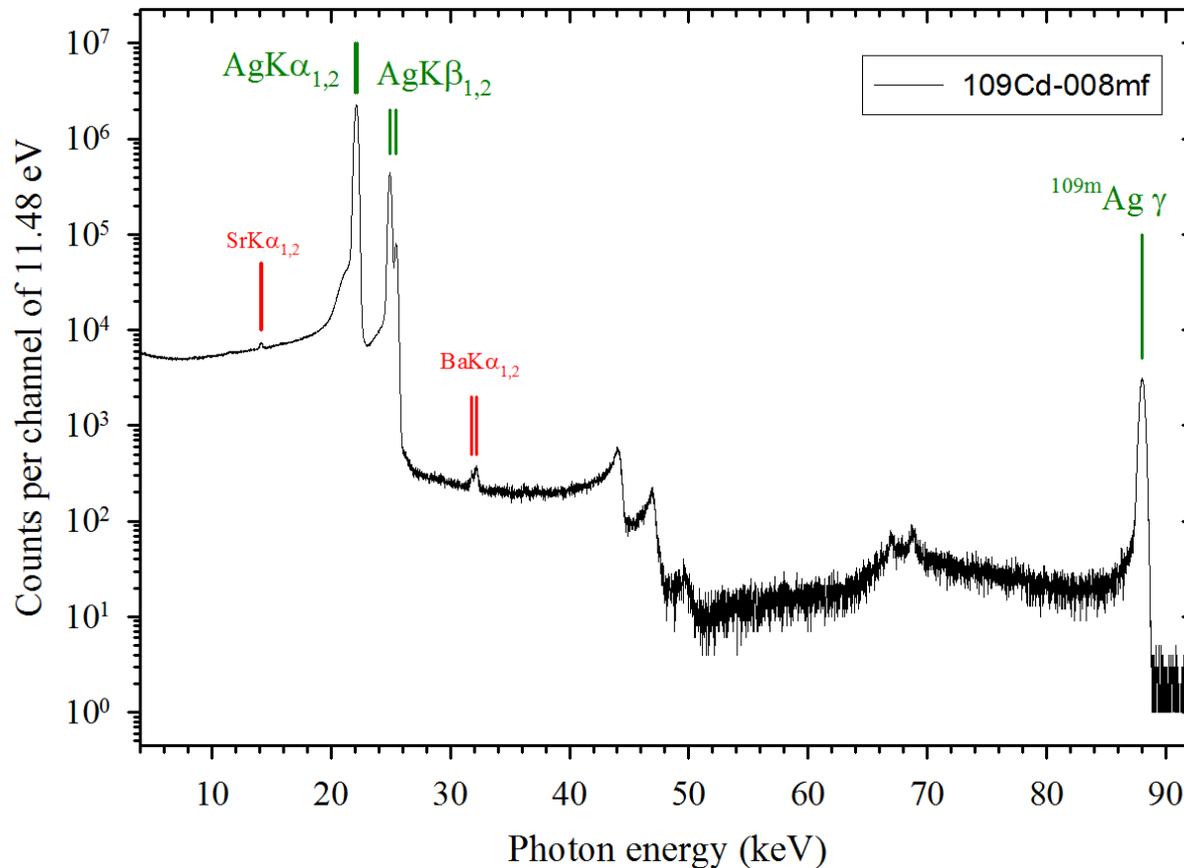
-88.0-keV E3 γ ray

$$\frac{\varepsilon_{\gamma}}{\varepsilon_K} = \frac{\omega_K(\alpha_K P_{\gamma} + P_{ec,K})}{P_{\gamma}} \cdot \frac{N_{\gamma}}{N_K}$$



Absolute efficiency calibration of the Si(Li) detector

Step 1: A ^{109}Cd source of known activity was put in front of the Si(Li) detector. This source emits K x rays of silver as well as 88.0336(10) keV gammas.



Absolute efficiency calibration of the Si(Li) detector

Step 2: For the K x rays of silver and for the 88.0336(10) keV gammas the *absolute efficiency* of the detector was found based on the *measured numbers of counts* in the corresponding peaks and the *known activity* of the source.

Step 3: The obtained results were compared to those *calculated* using **CYLTRAN†** Monte Carlo electron and photon transport code, taking into account the positions, shapes, sizes and materials of the detector and source components.

† J. A. Halbleib et al., Report SAND91-16734 (SNL, Albuquerque, 1992).

Absolute efficiency calibration of the Si(Li) detector

Step 4: We *modified* the values in the CYLTRAN *input* file for the position and effective thickness of the silicon crystal inside the detector so that the calculated efficiencies *match* the measured ones almost exactly (well within the statistical uncertainties).

thickness:	5.5 mm	--> 5.08 mm	(-0.42mm)
position:	7 mm	--> 10.4 mm	(+3.4mm)

Step 5: CYLTRAN was used to *calculate* absolute efficiencies for *niobium* K x rays and the 30.77 keV gammas, after making small adjustments in the input file for the position and size of the source.

Determination of relative efficiency

- Although absolute efficiencies calculated by CYLTRAN are sensitive to the variations of the input parameters, the relative efficiencies are sensitive much less.
- By considering reasonable variations of the input parameters, we concluded that *the relative efficiency that we need in this work is accurate within 0.5 %*.

Determination of α_K

$$\alpha_K = \frac{N_K}{N_\gamma} \cdot \frac{\epsilon_\gamma}{\epsilon_K} \cdot \frac{1}{\omega_K}$$

$$N_K = 3.0865(23) \text{ E}8 \text{ [0.074\%]}$$

$$N_\gamma = 1.179(51) \text{ E}4 \text{ [4.3\%]}$$

$$\omega_K = 0.751(4) \text{ [0.53\%]}$$

$$\epsilon_\gamma / \epsilon_K = 0.7200(36) \text{ [0.50\%]}$$

$$\alpha_K = 2.51(11) \text{ E}4 \text{ [4.4 \%]}$$

(from the data above)

$$\alpha_K = 2.62(15) \text{ E}4 \text{ [5.7\%]}$$

(from the remaining data)

$$\alpha_K = 2.55(9) \text{ E}4 \text{ [3.5\%]}$$

(combined result)

Comparison with calculations

With correction for self-absorption [x 0.9974(13) (-0.26%)]:

$\alpha_K = 2.54(9)E4$ [3.5%] (our preliminary final result)

The calculations predict

$\alpha_K = 2.39(4) E4$ (ignoring K vacancy in the final state)

$\alpha_K = 2.60(4) E4$ (including K vacancy in the final state)

==> Our results agrees with the calculations in which effects of the K vacancy in the final state are taken into account.